

# Role of cationic size in the optical properties of the LiCl crystal surface: theoretical study

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Received: 10 June 2011 / Accepted: 4 October 2011 / Published online: 28 October 2011  
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**Abstract** The size of the cations (either  $\text{Ca}^{2+}$ ,  $\text{Sr}^{2+}$ ,  $\text{Ga}^+$ , or  $\text{Au}^+$ ) at the  $F_{A1}$ -type color centers on the (100) surface of LiCl crystal plays an important role in the optical properties of this surface. In this work, double-well potentials at this surface were investigated using ab initio quantum mechanical methods. Quantum clusters were embedded in simulated Coulomb fields that closely approximate the Madelung fields of the host surface, and the ions that were the nearest neighbors to the  $F_{A1}$  site were allowed to relax to equilibrium. The calculated Stokes-shifted optical transition bands, optical–optical conversion efficiency, and relaxed excited states of the defect-containing surface, as well as the orientational destruction of the color centers, recording sensitivity, exciton (energy) transfer, and the Glasner–Tompkins empirical relation were all found to be sensitive to the size of the dopant cation.

**Keywords** Optical properties · LiCl surface ·  $F_{A1}:\text{Ca}^{2+}$  ·  $F_{A1}:\text{Sr}^{2+}$  ·  $F_{A1}:\text{Ga}^+$  ·  $F_{A1}:\text{Au}^+$

## Introduction

The modeling of solid-state processes has reached the stage at which it can be usefully employed for applications in solid-state chemistry and physics. Theoretical modeling is an especially powerful tool when searching for new

materials, as it can narrow down the list of potential materials for which crystal growth techniques need to be developed. The application of theoretical models would provide benefits when testing laser light generation. There have been a few detailed theoretical studies of the key processes associated with color center lasers. Such studies can suggest paths to new systems or to improvements in existing systems.

In the work described in the present paper, we considered how the size of the cations at some selected color centers on the regular surface of LiCl crystal influences the luminescence activities of such color centers. Aside from the data for the  $F_{A1}:\text{Sr}^{2+}$  color center reported by Abdel Aal [1], neither theoretical nor experimental data are currently available for the  $F_{A1}$ -type color centers present on the surface of LiCl. However, experimental investigations have been carried out for Sr-doped NaCl crystal by Joshi and Kekan [2] and the polycrystalline ceramic  $\text{Sr}_2\text{FeMoO}_6$  by Greneche et al. [3].

An F center consists of an anion vacancy binding an electron, while the more complex  $F_A$  center is an F center attached to a cationic impurity. In  $F_A$  centers [4], the threefold-degenerate  $2p$  state of the F center is split during absorption due to the adjacent cationic impurity, thus forming two well-resolved absorption bands,  $F_{A1}$  and  $F_{A2}$ . Two types of centers can therefore be distinguished, corresponding to the different relaxation behaviors of the centers after optical excitation. In type  $F_{A1}$  centers, the F center is attached to a large cationic impurity; in type  $F_{A2}$  centers, the F center is attached to a small cationic impurity relative to the host cation.

As far as laser light generation is concerned, electron–phonon coupling causes broadened Stokes-shifted optical transition bands. The electrons associated with a defect interact strongly with the surrounding vibrating crystal ions,

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resulting in optical transitions, which are allowed in a broad band around the defect-specific central transitions. All of the color center lasers realized so far are based on electronic defects. In 1991, Gellerman [5–8] reviewed some of the optical and laser properties of the most important examples of color center species in alkali halide crystals, and reported that color centers in these crystals can be applied as high-gain active materials in tunable solid-state lasers. Using various color center types and host lattices, the combined tuning range of color center lasers covers the near-infrared region from about 0.8 to 4  $\mu\text{m}$ .

The possible energy level structure for the electron at an  $F_A$  center is influenced by the shape and depth of the electronic binding potential. This potential is determined mainly by the distance and geometrical arrangement of the nearest surrounding lattice ions, which oscillate around their equilibrium positions. Therefore, the potential changes dynamically with the vibrations of the ions. This in turn modifies the electronic energy levels and charge distributions. The ionic equilibrium varies with the electronic state, and the electron–phonon coupling and its effect on the optical transitions can be illustrated using a configuration coordinate diagram [9].

The development of color center lasers depends on investigations of known color center systems with more favorable optical properties as well as the development of new laser-active defects. It appears that a laser-suitable defect should have the following properties: (1) one electron defect center, (2) compact electronic states, (3) relaxed excited states deep below the conduction band, and (4) it should be possible to experimentally produce such centers in high concentrations ( $\geq 5 \times 10^{16} \text{ cm}^{-3}$ ) [10].

Ab initio calculations of laser light generation at the ionic crystal surface are still lacking, and until recently the potential of  $F_{A1}:\text{Ga}^+$ ,  $\text{Au}^+$ , and  $\text{Ca}^{2+}$  center systems to supply useful laser action at the (100) surface of LiCl has been ignored [11–13]. We have therefore carried out a fairly extensive set of ab initio calculations in an attempt to examine the role of cationic radii of the doping cations  $\text{Ga}^+$ ,  $\text{Au}^+$ ,  $\text{Ca}^{2+}$ , and  $\text{Sr}^{2+}$  in laser light generation at the (100) surface of LiCl. Several related optical properties were also considered.

We have not been able to find any experimental data on the characteristics of laser light generation by the color centers of interest at the LiCl surface. Hence, our results serve as theoretical predictions.

The present study is organized as follows. “**Methods**” gives a brief account of the theoretical methods, namely, simulation of the low coordination (100) surface of LiCl, configuration interaction singles (CI singles), and configuration coordinate diagrams (CC diagrams). In “**Results and discussion**,” the results for laser light generation by the double-well potentials of the  $F_{A1}:\text{Ga}^+$ ,  $\text{Au}^+$ ,  $\text{Ca}^{2+}$ , and  $\text{Sr}^{2+}$

color centers are given and discussed. The results are then summarized and conclusions are drawn.

## Methods

### Crystal simulation

There are several methods that can be employed to simulate crystals, using either finite or infinite systems [14–19]. In the case of finite systems, only local portions of the crystal are considered. For such an approach, clusters of varying sizes in the bulk structure are suitable approximations. In the present study, we used a finite system to simulate the LiCl crystal.

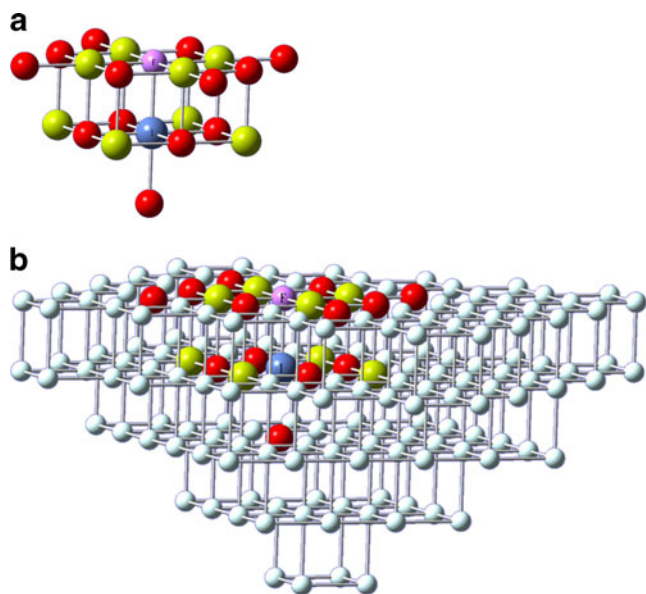
### Bulk simulation

A finite ionic crystal with 288 point charges was first constructed. The Coulomb potentials along the  $X$  and  $Y$  axes of this crystal were zero due to the symmetry of the host crystal. The  $\pm 1$  charges on the outer shells were then modified, using a fitting procedure, to make the Coulomb potential at the four central sites closely approximate the Madelung potential of the host crystal, and to make the Coulomb potential at the eight points with coordinates  $(0, \pm R, \pm R)$  and  $(\pm R, 0, \pm R)$ , where  $R$  is half the lattice distance (which for LiCl is 2.57 Å), equal to zero, as it is in the host crystal. When the resulting charges (0.409283 and 0.800909) are used, the Coulomb potential in the region occupied by the central ions is very close to that in the unit cell of the host crystal. The Coulomb potential was calculated to be 1.748 at the four central sites (compared with 1.746 for a simple cubic ionic crystal) and 0.0 at the previously defined eight points (compared with 0.0 for the same crystal).

### Surface simulation

All charged centers with Cartesian coordinates  $(\pm X, \pm Y, Z > 0)$  were eliminated to generate the (100) surface of LiCl, with 176 charged centers occupying the three-dimensional space  $(\pm X, \pm Y, Z \leq 0)$ . The clusters shown in Fig. 1 were then embedded within the central region of the crystal surface. All of the electrons of the embedded clusters were included in the Hamiltonians of the ab initio calculations. Other crystal sites entered the Hamiltonians as either full or partial ionic charges.

To account for the significant chemical effects associated with the creation of the defect, the clusters adopted to describe the  $F_{A1}:\text{Ga}^+$ ,  $\text{Au}^+$ ,  $\text{Ca}^{2+}$ , and  $\text{Sr}^{2+}$  color centers that generate laser light at the LiCl surface were denominated  $[\text{Li}_8\text{Cl}_{13}\text{F}_{A1}]$  (Fig. 1).



**Fig. 1** **a** Representative sketch of the surface clusters considered in the calculations. Red Cl<sup>-</sup>, yellow Li<sup>+</sup>, pink (F) F center, blue (I) impurity cation. **b** Representative sketch of the surface clusters embedded in point charges. Red Cl<sup>-</sup>, yellow Li<sup>+</sup>, pink (F) F center, blue (I) impurity cation

Calculations

Configuration coordinate diagrams

The geometric relaxation of F<sub>A</sub> centers in the ground and excited states is key to laser activity due to vibronic coupling. In other words, the possible energy level structure of the F<sub>A</sub> center electron is influenced by the shape and depth of the electronic binding potential. This potential is determined mainly by the geometrical arrangement of the nearest surrounding lattice ions, which oscillate around their equilibrium positions. The ionic equilibrium varies with the electronic state, and the electron–phonon coupling and its effect on the optical transitions can be illustrated using the well-known configuration coordinate diagram [20]. In the configuration coordinate diagram, the electronic energies in the ground and excited states are plotted versus the configuration coordinate *Q*, which represents a certain

localized or normal mode of the lattice coupling to the electron. In other words, *Q* represents the simultaneous displacement of the cations that are the nearest neighbors to the defect site from the lattice interionic separation (*Q*=0.0) along the axes joining them with the defect site. This is called the symmetric (or linear) coupling mode. The other ions were retained at their original positions in the lattice. Starting from the ground state of the F<sub>A</sub> center, an optical excitation produces a transition into the excited state at fixed nuclear coordinates assuming the Franck–Condon principle (i.e., vertical transitions in the configuration coordinate diagram). Due to the Gaussian-shaped probability function for the lowest vibrational state, the transition most probably starts from the equilibrium position *Q*<sub>1</sub>. The electronic distribution reached immediately after excitation is not in equilibrium with the lattice at *Q*<sub>1</sub>. As a consequence, the ions oscillate toward a new equilibrium position. The vibrational energy will be dissipated via anharmonicity into lattice phonons, and the lattice will reach the new equilibrium position *Q*<sub>2</sub>, i.e., the relaxed excited state. After the mean lifetime has elapsed, the excited electron returns by a vertical emission process to the ground state, and the subsequent lattice relaxation completes the optical cycle [5–8]. To construct the configuration coordinate diagrams, the ion clusters representing the F<sub>A1</sub>:Ga<sup>+</sup>, F<sub>A1</sub>:Au<sup>+</sup>, F<sub>A1</sub>:Ca<sup>2+</sup>, and F<sub>A1</sub>:Sr<sup>2+</sup> centers on the (100) surfaces of LiCl were first embedded into the three-dimensional arrays of the point ions described in the “Surface simulation” section. The representations of the ion clusters are given in Fig. 1. The absorption and emission energies were then calculated as the difference between the total energies of the ground and excited states. To achieve this, the relevant potential energy curves were calculated, and then—according to the Franck–Condon principle—the absorption energy was calculated as that for a vertical transition from the minimum of the relaxed ground state to the excited state. The luminescence energy was calculated in a similar manner. Stokes shifts were then calculated as the difference between absorption and emission energies:

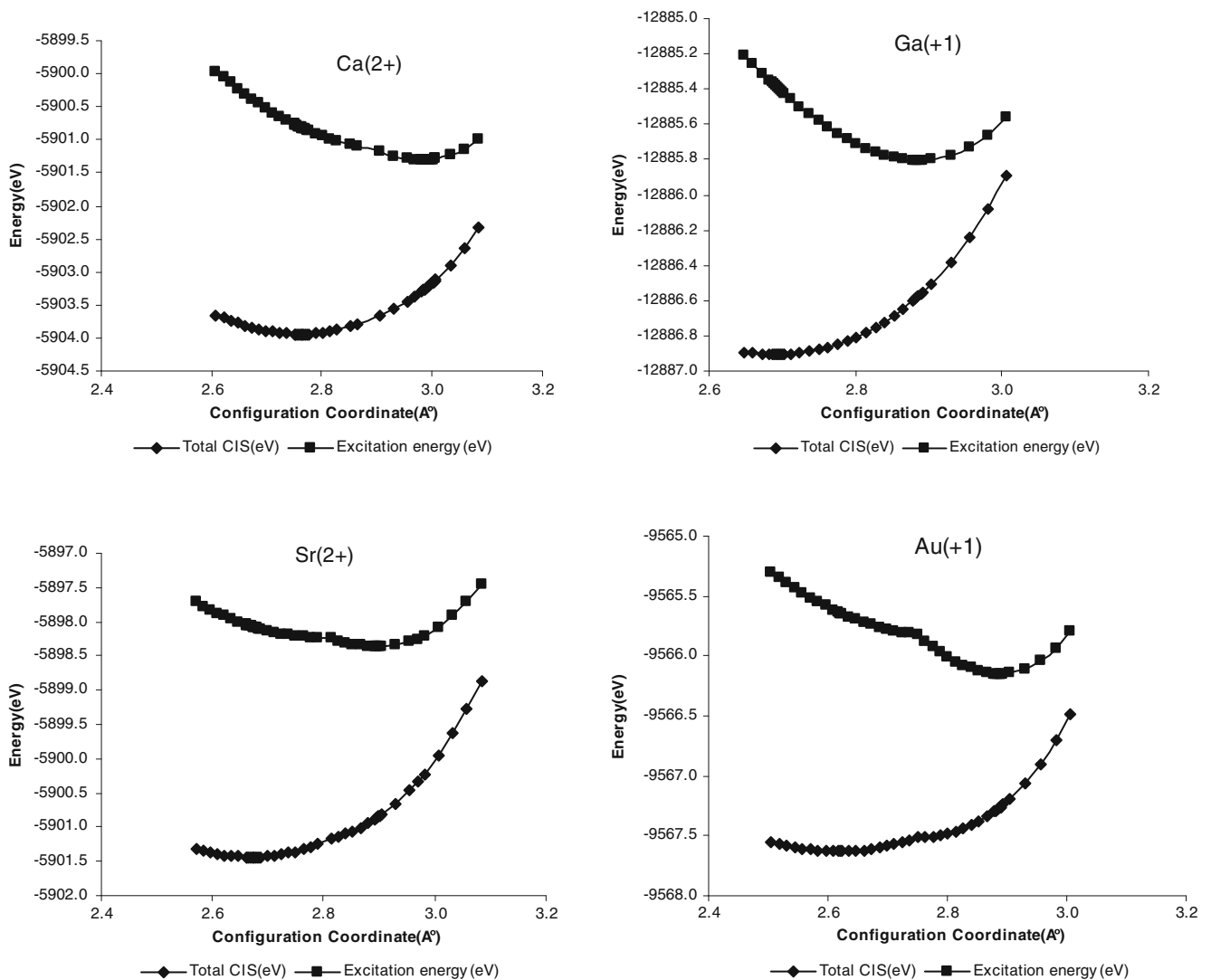
$$\Delta E_{\text{absorption}} - \Delta E_{\text{emission}}$$

**Table 1** The minima for the ground states (*Q*<sub>1</sub>) and low-lying excited states (*Q*<sub>2</sub>), horizontal shifts along the configuration coordinate (*Q*<sub>2</sub> – *Q*<sub>1</sub>), and absorbed and emission transition energies  $\Delta E$  between the

ground electronic states (g) and the low-lying excited electronic states (e) of F<sup>+</sup><sub>A</sub> centers at the (100) surface of LiCl crystal, calculated at the CIS level. *R*=1.285 Å, and energies are in eV

Crystal	Impurity	<i>Q</i> <sub>1</sub> / <i>R</i>	<i>Q</i> <sub>2</sub> / <i>R</i>	( <i>Q</i> <sub>2</sub> – <i>Q</i> <sub>1</sub> )	$\Delta E_{\text{absorption}}$	$\Delta E_{\text{emission}}$	Stokes shift
LiCl	Ga <sup>+</sup>	2.518	2.886	0.368	1.9368	0.7787	1.1581
	Au <sup>+</sup>	2.625	2.881	0.256	1.9742	1.146	0.8282
	Ca <sup>2+</sup>	2.758	2.985	0.227	3.1459	1.9713	1.1746
	Sr <sup>2+</sup> <sup>a</sup>	2.672	2.896	0.224	3.3631	2.4914	0.8717

<sup>a</sup> Reproducible data that were identical to those in [1]



**Fig. 2** Configuration coordinate diagrams for the  $F_{A1}:Ga^+$ ,  $F_{A1}:Cu^+$ ,  $F_{A1}:Ca^{2+}$ , and  $F_{A1}:Sr^{2+}$  laser color centers on the (100) surface of LiCl

### Configuration interaction singles method

The configuration interaction singles method was employed to calculate the  $F_A$  laser activity, the relaxed excited state orientational destruction of the  $F_A$  center, and the reorienta-

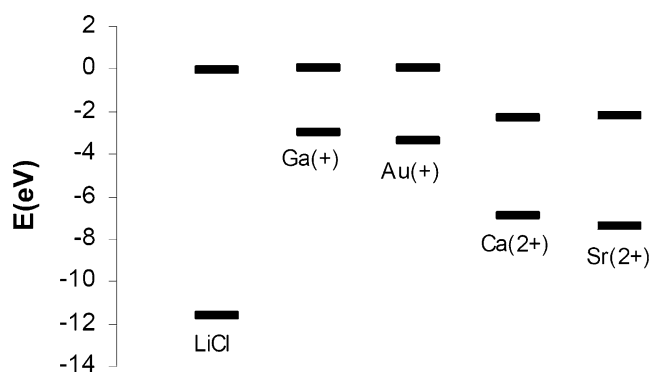
tional efficiency. The configuration interaction singles method uses the configuration interaction approach and models excited states as combinations of single substitutions out of the Hartree–Fock ground state. The CI singles theory is an adequate zeroth-order treatment for many

**Table 2** The tops of the valence bands (VBs) and the bottoms of the conduction bands (CBs) of the defect-free (100) surface in the ground electronic state, and the highest occupied molecular orbitals (HOMOs)

and the lowest unoccupied molecular orbitals (LUMOs) of the defect-containing (100) surface in the relaxed excited electronic state. The energies are calculated at the CIS level and given in eV

Crystal	Defect-free surface ground electronic state		Defect-containing bulk and surface relaxed excited electronic state		
	VBs	CBs	Impurity	HOMOs	LUMOs
LiCl	-11.630	-0.049	$Ga^+$	-3.006	0.0498
			$Au^+$	-3.419	0.0223
			$Ca^{2+}$	-6.939	-2.271
			$Sr^{2+}$ <sup>a</sup>	-7.463	-2.251

<sup>a</sup> Reproducible data that were identical to those in [1]



**Fig. 3** Representation of the data in Table 2. The tops of the valence bands (VBs) and the bottoms of the conduction bands (CBs) of the defect-free (100) surface in the ground electronic state, and the highest occupied molecular orbitals (HOMOs) and the lowest unoccupied molecular orbitals (LUMOs) of the defect-containing (100) surface in the relaxed excited electronic state

excited states of molecules. Treatments of large molecular systems can be made practical by avoiding integral storage and transformation, and thus the configuration interaction singles method has a wide range of applicability. A satisfactory exploration of the potential energy surfaces and the accurate electronic properties of excited states can be achieved using an analytic configuration interaction singles gradient [21, 22]. This method includes some electron correlation in the excited states, but can provide reasonable accuracy for excitation energies in comparison with the simplest way of finding the lowest relaxed excited state in wide gap insulators—self-consistent field calculations of the triplet state [23]. Note that Sousa and Illas [24] have examined the impact that a proper electron correlation treatment could have on the optical absorption energy of F centers in MgO.

#### Compact effective potential basis sets

The Stevens, Basch, and Krauss compact effective potential (CEP) basis sets [25–27] were employed in the present calculations. In these CEP basis sets, double-zeta calculations are referred to as CEP-31 G and triple-zeta

calculations as CEP-121 G. It should be noted that only one CEP basis set is defined beyond the second row, and the two basis sets are equivalent for these atoms. These basis sets have been used to calculate the equilibrium structures and spectroscopic properties of several molecules, and the results obtained compare extremely favorably with the corresponding all-electron calculations. The computations reported in this paper were carried out using the Gaussian 98 system [28].

## Results and discussion

### Stokes shifts

The configuration coordinate data for the  $F_{A1}:Ga^+$ ,  $Au^+$ ,  $Ca^{2+}$ , and  $Sr^{2+}$  laser color centers on the (100) surface of LiCl are given in Table 1, and the corresponding configuration coordinate curves are shown in Fig. 2. The strength of electron–phonon coupling as reflected by the value of the Stokes shift between the ground state and the low-lying excited state suggests that laser light generation is sensitive to the size of the impurity cation. Greater Stokes shifts are assigned to smaller cationic radii as follows:  $F_{A1}:Ga^+$  is greater than  $F_{A1}:Au^+$ , and  $F_{A1}:Ca^{2+}$  is greater than  $F_{A1}:Sr^{2+}$ . This is in agreement with the values of  $(Q_2 - Q_1)$ . In addition, the smallest Stokes shift is assigned to the  $Au^+$  ion, which has the largest electronegativity value and the smallest cationic size. Moreover, the Stokes shifts assigned to  $Ga^+$  and  $Ca^{2+}$  as well as those assigned to  $Au^+$  and  $Sr^{2+}$  are very similar, implying that (1) the potential of  $Ga^+$  for laser light generation is similar to that of  $Ca^{2+}$ , and ditto for  $Au^+$  and  $Sr^{2+}$ , and (2) sites with  $Ga^+$  and  $Ca^{2+}$  are more laser active than those with  $Au^+$  and  $Sr^{2+}$  based on the magnitude of each Stokes shift.

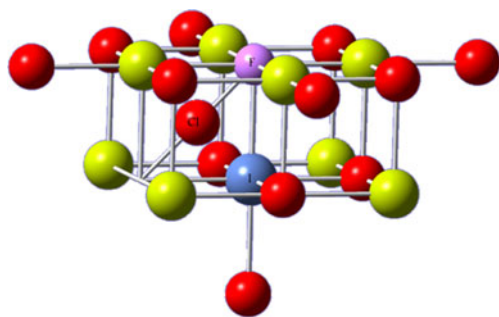
### Optical–optical conversion

With a small Stokes shift, the optical–optical conversion efficiency will be enhanced. On the other hand, the reabsorption of emitted light by other  $F_A$  centers will also

**Table 3** Energy barriers to the orientational destruction of the  $F_A^+$  center on the (100) surface of LiCl due to the migration of the bulk anion to the assumed saddle-point ion configuration. The energies are calculated at the CIS level

Crystal	Impurity	Total energy of the original RES ion configuration ( $E_h$ )	Total energy of the saddle point ion configuration ( $E_h$ )	Energy barrier ( $E_h$ )	Energy barrier (eV)
LiCl	$Ga^+$	−473.568353859	−473.401667058	0.167	4.536
	$Au^+$	−351.567017457	−351.432625826	0.134	3.657
	$Ca^{2+}$	−216.879914144	−216.759194681	0.121	3.285
	$Sr^{2+}$ <sup>a</sup>	−216.772094132	−216.611434261	0.161	4.372

<sup>a</sup> Reproducible data that were identical to those in [1]



**Fig. 4** Representation of the assumed relaxed excited-state saddle-point ion configuration responsible for the orientational destruction of the  $F_A$  center in the laser experiment. Red  $Cl^-$ , yellow  $Li^+$ , pink ( $F$ ) center, blue ( $I$ ) impurity cation

increase. If the negative effect of reabsorption is stronger than the positive effect due to the conversion efficiency, then the laser activity decrease. Inspecting Table 1 reveals that the negative effect of reabsorption is expected to be stronger than the positive effect of a smaller cationic radius.

A laser-suitable defect should have relaxed excited states deep below the conduction band of the perfect crystal [11–13]. To examine this issue, we consider the band structure of the LiCl surface (i.e., the positions of the one-electron defect levels with respect to the perfect surface bands). In Table 2 and Fig. 3, we present the tops of the valence bands and the bottoms of the conduction bands for the ground states of the defect-free surfaces, as well as the highest occupied molecular orbitals and the lowest unoccupied molecular orbitals for the relaxed excited states of the defect-containing surfaces. As shown in Table 2 and Fig. 3, the excited states are below the lower edges of the conduction bands of the defect-free surfaces, implying that all of the present color centers are laser-suitable defects.

#### Orientalional destruction

One consequence of the relaxed excited-state saddle-point ion configuration of the  $F_A$  center is a temperature-independent ionic reorientation during the pump cycle; i.e., a change of the center axis to a perpendicular (equivalent) orientation. After the emission process, the assumed saddle-point ion has

a 50% chance of hopping to the  $\langle 110 \rangle$  anion vacancy site opposite its starting location. Therefore, if the  $F_A$  center system is excited in either one of its absorption bands by polarized light with a direction of propagation parallel to the  $\langle 100 \rangle$  axis and its electric field vector  $E$  parallel to the perpendicular  $\langle 100 \rangle$  axis, the  $F_A$  centers excited by this  $E$  vector will quickly be reoriented to the  $\langle 100 \rangle$  direction, at which point the  $F_A$  centers will no longer be excited, and this reoriented system will become experimentally transparent for the excitation light [5–8]. However, it has been observed experimentally and theoretically by many workers that no spectral region in the absorption range of the  $F_A$  band is completely transparent, even after prolonged preferential optical excitation of the  $F_A$  centers.

To theoretically examine the relaxed excited-state orientational destruction of the  $F_A$  center, we calculated the total energies of the original relaxed excited-state ion configuration and the assumed saddle-point ion configurations of the present color centers on the (100) surface of LiCl. The differences between the energies of these configurations (the energy barriers to orientational bleaching in a laser experiment) are given in Table 3 and are shown in Fig. 4. There is no clear dependence of the energy barrier on the cationic radius of the dopant. However, it is clear from the data in Table 3 that the value of the energy barrier due to the migration of the anion species to the vacancy site in the case of  $Ga^+$  is very similar to that seen for  $Sr^{2+}$ , and the difference in the energy barriers for  $Au^+$  and  $Ca^{2+}$  ( $3.657 - 3.285$  eV) is only 0.38 eV. In other words, orientational destruction is generally probable for this type of  $F_A$  centers, particularly  $F_{A1}:Ca^{2+}$ , which has the highest reported Stokes shift. Experimentally, in order to avoid orientational bleaching, the pump polarization and the direction of propagation of the pump beam inside the crystal must be chosen such that they are not parallel to the  $\langle 100 \rangle$  direction.

#### Optical memories

It is possible to use the reorientation of a defect such as an  $F_A$  center under the action of polarized light to store information [9, 10].  $F_A$  centers can easily reorient at relatively low temperatures, and the reorientation efficiency is

**Table 4**  $F_A^+$  band gap  $E_{FA}^+$  and exciton band  $E_X$  on the (100) surface of LiCl. The energies are calculated at the DFT level

Crystal	Impurity	CB ( $E_h$ )	VB ( $E_h$ )	$E_{FA}^+$ ( $E_h$ )	$E_{FA}^+$ (eV)	$E_{normal}$ ( $E_h$ )	$E_{exciton}$ ( $E_h$ )	$E_X$ ( $E_h$ )	$E_X$ (eV)	$E_X - E_{FA}^+$ (eV)
LiCl	$Ga^+$	-0.086	-0.054	-0.032	-0.866	-478.214	-477.723	0.491	13.366	12.875
	$Au^+$	-0.100	-0.057	-0.043	-1.182	-355.950	-355.459	0.492	13.380	12.888
	$Ca^{2+}$	-0.252	-0.139	-0.113	-3.079	-220.417	-219.954	0.463	12.610	12.147
	$Sr^{2+a}$	-0.252	-0.138	-0.114	-3.109	-220.329	-219.863	0.465	12.664	12.199

<sup>a</sup> Reproducible data that were identical to those in [1]

$E_{FA}^+ = CB - VB$ ,  $E_X = E_{exciton} - E_{normal}$

very high above 140 K, which implies high recording sensitivity. However, at 55 K, this efficiency practically vanishes; thus, it is possible to “read” with polarized light. In the dark, there is no thermal reorientation of the centers, and thus the information may be stored indefinitely. As shown in Table 3, the reorientation efficiency (probability) of  $F_A$  centers due to the migration of the bulk anions to the assumed saddle-point ion configuration increases as the size of the impurity cation increases from  $Ga^+$  to  $Au^+$  and from  $Ca^{2+}$  to  $Sr^{2+}$ . This implies a high recording sensitivity for  $F_{A1}:Ga^+$  relative to  $F_{A1}:Au^+$ , and for  $F_{A1}:Ca^{2+}$  relative to  $F_{A1}:Sr^{2+}$ . Indeed, the highest recording sensitivity is assigned to  $F_{A1}:Ga^+$ , as it has the largest energy barrier.

#### Glasner–Tompkins relation

Glasner and Tompkins [29] reported an empirical relationship between the principal optical absorption of F centers in solids and the fundamental absorption of the host crystal. The difference between the first exciton absorption energy  $E_X$  and the F-band energy  $E_F$  was found to depend almost exclusively on the negative ion species. In other words, the Glasner–Tompkins empirical rule suggests that the energy difference between the fundamental absorption of an alkali halide and the F band is very nearly only a function of the halide species. Exciton band  $E_X$ , F-band  $E_F$ ,  $(E_X - E_F)$  and  $\langle(E_X - E_F)\rangle$  values for twelve alkali halides have been reported by Malghani and Smith [30] and for LiH and LiF by Shalabi et al. [31]. The dependence of the Glasner–Tompkins relation on the impurity cation and the surface coordination number (flat, edge and corner) has also been reported for MgO, KCl and AgBr by Shalabi et al. [11, 32]. However, no attempt has been made to clarify the dependence of the Glasner–Tompkins relation on the size of the impurity cation on the (100) surface of LiCl.

To apply the Glasner–Tompkins relation to the present  $F_A$  centers, we have to calculate the corresponding band gaps and exciton bands. A complete treatment of the host dependence of the band gaps would involve theories of excitons and defects [33–40] that take into account the band structure. Since this would be a major undertaking and well beyond our present goal, we used the simple electron transfer model of the fundamental optical absorption of ionic solids developed by Hilsch and Pohl [41]. This model, in its simplest form, explains the fundamental optical absorption EX as the transfer of an electron from a negative ion to a neighboring positive ion, both positioned adjacent to the defect site. It seems likely that all color centers have perturbed excitons that form nearby. We therefore calculated EX as the change in Coulomb energy associated with the transfer of an electron from a halide anion to a lithium cation, both of which are located adjacent to the  $F_A$  center,

and calculated  $E_{FA}$  as the energy difference between the highest occupied molecular orbital and the lowest unoccupied molecular orbital energy levels. The correlation between the surface ion coordination, the  $F_A$  center, and the energy difference between the exciton band  $E_X$  and the band gap  $E_{FA}$  is given in Table 4. The results shown in the table confirm that while the energy difference between the exciton band  $E_X$  and band gap  $E_{FA}$  is directly proportional to the radius of the dopant cation, it is inversely proportional to the electronegativity,  $F_{A1}:Au^+ > Ga^+ > Sr^{2+} > Ca^{2+}$ . This suggests that the difference between the first exciton absorption energy  $E_X$  and the F-band energy  $E_F$  depends on not only the anion species but also the size and electronegativity of the cation species.

#### Conclusions

The value of the Stokes shift between the ground state and the low-lying excited state suggests that laser light generation is sensitive to the size of the impurity cation. Greater Stokes shifts are assigned to smaller cationic radii as follows:  $F_{A1}:Ga^+$  is greater than that of  $F_{A1}:Au^+$ , and  $F_{A1}:Ca^{2+}$  is greater than that of  $F_{A1}:Sr^{2+}$ . Moreover, the Stokes shifts assigned to  $Ga^+$  and  $Ca^{2+}$  are very similar, and those assigned to  $Au^+$  and  $Sr^{2+}$  are nearly identical. An examination of the band structure of the LiCl surface (i.e., the positions of the one-electron defect levels with respect to the perfect surface bands) showed that the excited states are below the lower edges of the conduction bands of the defect-free surfaces, implying that all of the color centers considered in this work are laser-suitable defects. Calculations of the total energies of the original relaxed excited-state ion configuration and the assumed saddle-point ion configuration of each center suggest that the energy barrier to the migration of the anion species to the vacancy site in the case of  $Ga^+$  is very similar in size to that of  $Sr^{2+}$ , and the difference in the energy barriers of  $Au^+$  and  $Ca^{2+}$  is only 0.38 eV. Calculations of the Glasner–Tompkins relation for the present  $F_A$  centers indicated that the difference between the first exciton absorption energy  $E_X$  and the F-band energy  $E_F$  depends not only on the negative ion species but also on the size of the impurity cation.

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